

- Probability
- computing the probability of an event (permutations, combinations, union, intersection, etc.)
  - conditional probability (compute and interpret)
  - independence
  - Bayes' theorem

- Random Variables
- discrete vs. continuous
  - pdf and cdf
  - calculating probability of events from the pdf and cdf
  - expected values
  - moment generating functions
  - multivariate versions of all of the above
  - conditional distributions and conditional expectations,  $E[Y|X]$
  - covariance and correlation
  - independence
  - named distributions:
    - \* Bernoulli, binomial, geometric, multinomial
    - \* Poisson (including approximation to binomial, Poisson process)
    - \* exponential, gamma, chi-square
    - \* uniform
    - \* cauchy
    - \* normal (including bivariate and multivariate, and the distribution of  $\bar{X}$  and  $S^2$ , linear combinations of  $X_i$ 's)
    - \* beta
    - \*  $t$
    - \* F
  - transformations (cdf method, Jacobian, MGF method)
  - statistics, order statistics, random samples
  - convergence:
    - \* in distribution
    - \* in probability
    - \* WLLN, SLLN
    - \* MGF's, Slutsky's theorem
  - Central limit theorem
  - delta method